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Assessing swells in La Réunion Island from terrestrial seismic observations, oceanographic records and offshore wave models

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SUMMARY

La Réunion Island in the southwest Indian Ocean is seasonally affected by austral swells among which some extreme events may have strong impacts on coastal infrastructures. The very limited number of sensors available on and around the island and in the whole SW Indian Ocean impedes any direct monitoring of the swell activity. In this study, we analyse direct observations of the ocean swell by combining terrestrial measurements of the microseismic noise with in situ oceanographic observations issued from two pressure gauges and an Acoustic Doppler Current Profiler (ADCP), together with swell numerical modelling. The reliability of the terrestrial seismic station to characterize the ocean activity in both the primary and secondary microseisms peaks (PM and SM, respectively), and also in the long period secondary microseismic peak (LPSM) for the case of La Réunion Island is presented and discussed here. By computing the hourly RMS of the PM and LP(SM) amplitudes, we establish a transfer function between the PM and (LP)SM amplitude and the maximum wave height, which appears to be valid for any PM and LPSM amplitudes >0.15 μ m and >1.0 μ m, respectively. The correlation coefficient between the PM amplitude and the wave height is >0.92. It suggests that the PM amplitude can be used as a robust proxy for the swell height and may help calibrating the wave heights from other independent observable. For some swell events, we observe LPSM that correlate well (>0.91) with the local wave height suggesting a generation by coastal swell reflection. From polarization and spectral analyses, directions and periods of swells are also well retrieved from seismic data. Finally, continuous measure of the SM amplitude shows that it can be used as precursor information for distant swells that may hit La Réunion Island a few days after their generation in the southern Indian Ocean.

Key words: Indian Ocean; Seismic noise; Surface waves and free oscillations.

1 INTRODUCTION

La Réunion Island is located in the southwest (SW) Indian Ocean (Fig. 1). It is affected by sporadic oceanic swells generated by tropical cyclones (occurring mainly during summer periods, i.e. from November to March) or by austral swell events (observed in austral winter, from April to October). Austral swells that reach La Réunion Island are generated by distant storms in the Southern Indian Ocean at distance of 3000–4000 km (e.g. Davy *et al.* 2015). Generated by strong winds and long fetches within strong atmospheric depressions circulating around Antarctica, the swells may take a few days to reach La Réunion Island, where it may produce significant damage to the coastal infrastructures such as roads, houses, harbors, but also to the natural coral reef protecting part of the western coast of La Réunion (e.g. Cordier *et al.* 2012). Monitoring the swell activity around the island and in the SW Indian Ocean is therefore of broad interest but is strongly limited by the little number of oceanographic sensors available. To extend the work of Davy *et al.* (2014, 2015, 2016) and Barruol *et al.* (2016), we analyse the ocean-induced microseismic noise recorded by terrestrial seismic stations installed on La Réunion Island, and we combine those observables with *in situ* ocean observations issued from two pressure sensors (OSSI, Ocean Sensor Systems Inc.) deployed in the fringing reef and off shore, and an ADCP (Acoustic Doppler Current Profiler, Nortek Aquadopp Profiler) deployed off shore (Figs 1b and c).

Microseisms have been long known to be generated by ocean gravity waves (e.g. Longuet-Higgins 1950) and can be recorded by seismic stations worldwide. The existence of two types of microseisms—the Primary and Secondary Microseisms (PM and SM, respectively), which differ from their dominant periods and



origins-is broadly accepted despite their origins and the involved processes are still actively studied (e.g. Ardhuin et al. 2011, 2015). PM are accepted to occur in coastal waters and concentrate the energy at the same period as the ocean swell, that is at periods $\sim 10-$ 20 s (frequencies between 0.05 and 0.10 Hz). They are interpreted as the interaction between sloping seafloor and the approaching ocean waves (e.g. Hasselmann 1963; Barruol et al. 2006; Ardhuin et al. 2015). On the other hand, SM are accepted to be generated within the ocean basins by the interaction of two swells of same periods propagating in opposite directions (e.g. Longuet-Higgins 1950), generating standing waves and vertical pressure variations across the water column, that excite seismic waves on the ocean bottom. SM therefore dominate at half the dominant swell periods, that is between \sim 3 and 10 s (frequencies between \sim 0.10 and 0.33 Hz). SM sources have been located (1) in the open ocean where standing waves are created by the interaction of two distant swells (e.g. Obrebski et al. 2012), (2) in coastal regions where a swell reflected at the coast may interact with the incoming waves (e.g. Ardhuin et al. 2011; Stutzmann et al. 2012; Bromirski et al. 2013), generating the so-called long period secondary microseism (LPSM) and (3) in a storm due to the interaction of two waves from opposite directions issued from the same system or waves issued from two different storms (e.g. Ardhuin et al. 2011; Obrebski et al. 2013; Davy et al. 2014).

In this study, we analyse a sequence of austral swells that hit La Réunion Island between 13 March and 5 May 2017.

On land, we analyse the seismological data to determine the dominant frequency of the PM and SM using the power spectral density analysis that may provide a link to the swell peak period T_p ; we quantify the microseismic amplitudes by computing an hourly root mean square (RMS) in each frequency band that provides information on the local or distant significant wave height H_s (in the case of the PM or SM band, respectively); we finally perform a polarization analysis to determine the dominant direction and strength of polarization of the recorded microseismic noise, that may indicate the wave peak direction D_p for the case of the PM band or the source direction in the SM band.

At sea, oceanographic sensors were deployed during this period inside and outside the fringing reef along the west coast of La Réunion Island: one sensor on the reef flat and two others on the reef external slope (Fig. 1). Such in situ measurements allowed us to derive the local wave heights and periods from bottom pressure gauges and the swell direction from the ADCP sensor. We used those oceanographic observations, together with the land seismological data and the WaveWatch III (WWIII) swell models to establish relations between the observed and modelled swell parameters. One of the objectives of this work is indeed to establish the relationship between the land-recorded seismological PM amplitudes and the ocean-observed significant wave height (H_s , measured by the OSSI pressure wave gauge) and to demonstrate that the PM can be used as a proxy of the H_s , and therefore, that a land seismometer can be used as a well calibrated swell gauge. We also evaluate the accuracy of the modelled swell direction, height and period (respectively $D_{\rm pm}$, $H_{\rm sm}$) and T_{pm} parameters) derived from numerical models (WWIII) in the west of La Réunion Island by comparing them with the observed parameters. These approaches allow us to compute the transfer function relating the microseism amplitudes (in the PM and LPSM bands) and the wave height derived from the wave gauges and modelled from WWIII. We finally show that analysing distant SM sources can provide precursory information of the swells impacting La Réunion Island.

2 SEISMIC DATA ANALYSES

This study uses data from the temporary deployment of 10 broadband seismometers from the 'Rivière des Pluies' network (Fontaine et al. 2015). Most of the stations deployed in the northern part of the island have been operated since 2016 and are installed along two hydrological basins in La Réunion Island: the Rivière des Pluies (RIV*) and Rivière du Mât (RMA*). These stations were initially deployed to study the erosion and the sediment transport in the flooding rivers during cyclones (Gonzalez 2019). The station SALI installed on the western shore of the island, in the very neighbourhood of the fringing reef was deployed in February 2017 and is in appropriate location to study the swell seismic signature (Fig. 1). We also used the data recorded by the permanent seismic stations (16 broad-band seismometers) of the Observatoire Volcanologique du Piton de la Fournaise (OVPF/IPGP). The seismic data are available at the RESIF data portal (http://seismology.resif.fr) under the FDSN network code ZF and PF for the temporary and permanent stations, respectively. In this work, we analysed the microseismic noise recorded by these stations between 13 March and 5 May 2017, as oceanographic sensors (pressures gauges and ADCP) were deployed near to La Réunion Island during this period (Fig. 1).

Three methods are used to analyse the microseismic noise.

(i) To constrain the swell period T_p in the neighbourhood of the island, we calculate the seismological power spectral density (PSD) in the PM frequency band. To compute the PSD, we selected 1-hr data with 50 per cent overlap; then, each 1-hr time-series was divided into 13 segments with 75 per cent overlap between neighbouring segments, and later transformed into the time–frequency domain using the method of McNamara & Buland (2004). The obtained PSD was finally converted into decibels with respect to acceleration. To compute the daily average PSD into decibels with respect to acceleration as a function of the frequency, the *sacpsd* command from Herrmann (2013) was used.

(ii) To estimate the wave height H_s , we measured the hourly root mean square (RMS) of the microseism amplitude. The information about the wave height that hit the coastal area can be found in the PM amplitude, while the SM amplitude gives us an insight about the wave height at the swell source location, that is within the storm where it is generated. To compute the RMS, we first converted the amplitude of the microseism into displacement (μ m) by removing the instrument response. Then, we divided the data into 1-hr segments and applied a Butterworth bandpass filter with corner frequencies of 0.05 and 0.10 Hz for the PM and 0.10 and 0.33 Hz for the SM. The hourly RMS of the microseism amplitude were then computed from the filtered data. Finally, we determined the correlation coefficients between the microseism amplitude and the wave height using the Pearson method (Pearson 1909). Estimating the significant wave height using seismic land station, have been successfully used before using different methods (e.g. Bromirski et al. 1999; Donne et al. 2014).

(iii) To characterize the swell direction D_p , we performed a polarization analysis using two methods: a complex polarization analysis (e.g. Vidale 1986) and a principal component analysis (e.g. Barruol *et al.* 2006; Fontaine *et al.* 2009). Both methods provided comparable values, so we only present results from the second approach. Analysing the polarization in the PM frequency band would give information regarding the swell direction before it breaks at the coastal area, while the polarization in the SM frequency band should give the information on the distant source (i.e. storm) backazimuth. Practically, we detrend and taper the three components (E–W, N–S



Figure 1. Location of the seismic stations and oceanographic instruments in La Réunion Island. (a) Blue and red triangles show the permanent (OVPF/IPGP, PF network) and temporary seismic network (Rivière des Pluies, ZF network). Diamonds indicate the location of the wave gauge from the Candhis network installed in Le Port harbour (magenta) and the OSSI pressure instruments offshore (cyan) and in the lagoon (green). Yellow diamond shows the location of the WW3 model node used in this study. Bathymetry data is from Délégation Ifremer océan Indien (2012) and 200 m isocontours are presented. (b) Green and cyan points indicate the pressure sensors located within the lagoon (MID, midreef) and the ADCP and pressure sensor deployed outside of the reef (OFF, offreef), respectively. SALI is the seismic station running on land close to the oceanographic instrumental transect. Yellow line shows the cross-section in subplot (c). The step of the bathymetric isocontour here is 5 m. (c) Schematic bathymetric cross-section illustrating the instrumental transect deployed from land (seismic station SALI) to the open ocean (ADCP + pressure sensor deployed on the external slope of the reef), passing through the lagoon (pressure sensor).

and vertical) of the seismic waveform before converting them into ground velocity by removing the station response. For this step, we divided the data into hourly segments. For each segment, we obtained the eigenvalues and eigenvectors from which we derived the different parameters such as 0° < backazimuth <360°, and the coefficient of polarization in the horizontal (0 < CpH < 1) and vertical (0 < CpZ < 1) planes (e.g. Barruol *et al.* 2006). *CpH* or *CpZ* equal to 0 indicates a circular polarization in the corresponding plane, whereas a value of 1 indicates a perfectly rectilinear polarization. These different parameters were defined in Fontaine *et al.* (2009) and allow us to characterize the full 3-D ground motion, which helps us to locate the source of the microseism and to quantify the strength of polarization.

3 OCEANIC WAVE DATA ANALYSES

Three types of oceanic wave data were used in this study, two from local, *in situ* observations, and one from numerical modelling (Fig. 1).

The first *in situ* data set was obtained from two ocean pressure sensors OSSI (Ocean Sensor Systems Inc) and from an ADCP (Nortek Aquadopp Profiler) deployed in the coastal area of La Réunion Island from 13 March to 5 May 2017 (Fig. 1). A first pressure sensor was installed inside the fringing reef at a depth of around 1 m (MID, Figs 1b and c) and a second one on the reef external slope at a depth of 20 m (OFF, Figs 1b and c). They were continuously recording the pressure induced by the sea surface variations at a sampling rate of 10 Hz. The pressure data were corrected from atmospheric mean sea level pressure and non-hydrostatic pressure following linear wave theory (Hom-ma *et al.* 1967). The tidal components were then removed from the computed water depth using a 2nd order Butterworth lowpass filter with 6-hr cut-off frequency. Finally, a spectral analysis was performed on the detided signal to determine the wave power spectral density, from which an hourly time-series of wave height and period was extracted. To measure the wave propagation direction, the OFF pressure sensor was coupled with the ADCP, that recorded the pressure P and the two components U, V of the subsurface velocities variations at 2 Hz in burst mode of 1024 s for each hour. To compute the wave parameters, the PUV method was used, which involves a cross spectral analysis of the pressure P and the orbital velocities U and V (Pedersen 2002; Sullivan *et al.* 2006).

The second *in situ* data set was obtained from the non-directional datawell wave buoy located at the 'Rivière des Galets', a coastal station installed at a depth of 33 m, as part of the Candhis (Centre d'Archivage National de Données de Houle In Situ) network (CAND, Fig. 1). The data are freely available at the Candhis website (http://candhis.cetmef.developpement-durable.gouv.fr) from which one can retrieve hourly time-series of significant wave height (H_s) and wave peak period (T_p).

Finally, the last data set used was an hourly forecast of wave parameters issued from the 0.5° resolution global wave model forecast distributed by the Pacific Islands Ocean Observing System (PacIOOS, http://www.pacioos.hawaii.edu/waves/model-global) and configured in the School of Ocean and Earth Science and Technology (SOEST) at the University of Hawaii. These forecasts are based on the WaveWatch III model developed by the National Oceanic and Atmospheric Administration (NOAA) and National Centers for Environmental Prediction (NCEP). The hourly significant wave height $(H_{\rm sm}, \text{ with m subscript used for model})$, peak period $(T_{\rm pm})$, peak direction for sea state (D_{pm}) and for swell component only (D_{pms}) were extracted at a node of the model located west of La Réunion Island, at latitude 21°S and longitude 55°E (point WW3, Fig. 1). The forecast parameters were used in this study because they have an hourly time step, which is similar to the observations and seismic data time steps. Also, as shown in Fig. S1, the data are comparable to the 3 hr hindcasts global wave model from IOWAGA Ifremer (Rascle & Ardhuin 2013).

4 SPECTRAL CHARACTERISTICS OF MICROSEISMS

The temporal evolution of the microseisms for station SALI derived from the PSD analysis between 13 March and 5 May 2017 is presented in Figs 2 and S2. These figures indicate that both the PM and SM have a higher level of energy during the swell events, and that SM dominates the signal.

The daily average PSDs are presented in Fig. 2(b) for the various individual swell events, selected by the white boxes on Fig. 2(a) at station SALI, occurring between 13 March and 5 May 2017. Compared to a quiet period without any austral swell (indicated by the spectrum measured on 21 March and 6 April 2017, dashed colored lines Fig. 2b), the increase of the microseismic noise during the occurrence of each swell is clearly observed in both the SM (up to 10 dB) and the PM bands (up to 30 dB) indicated by the different grey areas. Each swell event recorded at SALI has a clear signature in the PM band, the amplitude of which depends on the swell strength (Fig. 2).

The very low level of noise in the PM band in the absence of swell is shown for two different days (21 March and 6 April 2017), but the two corresponding daily spectra behave differently in the SM band. On April 6 (orange dashed line), the noise is very low in the SM band whereas on March 21 (pink dashed line), one can observe a peak of energy in the SM. This results from the fact that PM is known to be generated in shallow water, near coastal areas, due to a pressure variation at the bottom of the sea (e.g. Ardhuin et al. 2015) whereas the SM is sourced within storms at large distance in ocean basins. The high SM energy on March 21 likely indicates a distant storm that transmits the SM energy almost instantaneously at the seismic station, whereas the swell produced by this particular storm will reach the island only few days later. The presence of an individualized LPSM peak is observed for the April 28 event, which is the most energetic swell event visible on the spectrogram in Fig. 2. It has twice the frequency of the PM, suggesting its local origin, due to interaction of the wave reflected from the coast with the incident swell. Such a process likely generates standing waves in the near-coastal region and provides energy in the LPSM band to the ocean floor.

Fig. 2(c) presents the PSD calculated for the individual swell event of 28 April 2017, but at the various seismic stations on La Réunion Island. For this particular swell event, Fig. 2(c) indicates the presence of clear PM, LPSM and SM peaks at all island stations. The homogeneous PM amplitudes indicate that the swell energy propagates well across the island. The two distinct peaks observed at ~0.15 Hz (LPSM) and ~0.25 Hz (SM) suggest the presence of two source locations of secondary microseisms, with distinct dominant frequencies. Note that all of the stations recorded a comparable amount of noise during the occurrence of this swell event. The exception being for station FOR where the PM is very low compared to the other stations, likely explained by a site effect causing attenuation close to the station.

5 COMPARING SWELL DATA AND MICROSEISMS AMPLITUDES

The wave data time-series are illustrated in Figs 3 and S3 for the coastal in situ observations and the swell modelled from WWIII. In general, the $H_{\rm sm}$ modelled at site WW3 (in red Fig. 3a) displays a systematic higher amplitude compared to the actual coastal observations. Exception occurs on April 23 to 29 (Box F) during which the observed H_s offshore has the highest amplitude. This observation could be associated to the fact that the global wave model (resolution 0.5°) is relatively crude to represent coastal processes and that the waves modelled in the open ocean do not take into account refraction, diffraction and/or shoaling processes that occur at a local scale. In fact, the wave reflected from the coastal area (which produced the LPSM) attenuated rapidly and are likely to be weakly felt at the WWIII location (i.e. at latitude 21°S and longitude 55°E, WW3 node). However, despite these systematic amplitude differences, the time-series show very similar patterns with H_s peaks related to strong swell events occurring at the same time in the observations and in the models.

An important insight shown in Fig. 3(a) is the role of the reef as shore protector. The wave amplitudes are indeed reduced by a factor of ~ 10 when crossing the coral reef (see the 10 times smaller right vertical axis associated to the midreef H_s measurement as the pink curve) while preserving very well the overall amplitude variations. This observation is in agreement with the tidal amplitude attenuation in the reef described by Cordier *et al.* (2012) in the same area, and indicates that the swell recorded inside the lagoon (midreef) is a very good proxy of the swell recorded further in the open ocean.



Figure 2. Power spectral density (PSD) of seismic noise converted into decibels relative to ground acceleration. (a) Spectrogram of the vertical component of seismic station SALI from 13 March to 5 May 2017. White rectangles show the swell events we analysed in this work. The 10 s (0.10 Hz) period limit between PM and SM is marked by the horizontal dashed line. (b) Daily mean PSD of data recorded at station SALI (vertical component) during the occurrence of the austral swell events occurring between 13 March and 5 May 2017. The orange and pink dashed line indicates the PSD at this station during quiet days without swell. The source of the peak at 2 Hz observed at station SALI is not identified but is likely associated with anthropogenic activity in the site neighbourhood. (c) Mean PSD of the vertical components of the different stations in La Réunion for the austral swell that occurred on 28 April 2017. For reference, the high and low noise models from Peterson (1993) are plotted in black continuous and dashed lines, respectively. Grey shadings indicate the frequency domains of PM, LPSM and SM.

Also, this shows the mechanical importance of a coral barrier to attenuate strong swell events and hence to avoid significant damage to coastal infrastructures.

Another observation from Fig. 3(a) is that the amplitudes of the swell events are generally much smaller (except the event in box C) at the 'Rivière des Galets' station (CAND) compared to those measured at the offshore coastal reef measurements (OFF). These differences likely suggest that the direction of propagation of the incident waves significantly affects how the waves impact the shore. The CAND station is indeed located 20 km north of the fringing reef area where the pressure measurements are performed. As the swells arrive from the south or the southwest, they likely experienced refraction and diffraction processes along the coast of the island, thus reducing their energy before being recorded at the CAND station. Regarding the swell event of box C, its origin of propagation is slightly more westward, thus preventing the waves to be damped due to coastal processes before arriving at CAND station. Therefore, to better monitor the Austral swell activity in La Réunion Island, it may be useful to have a buoy installed in the south.

The pattern of the PM and SM variations together with the observed H_s are presented in Figs 3(b) and (c), respectively, and also in Fig. S4. In general, for the austral swell events, the PM amplitude and the observed H_s display very similar trends (Fig. 3b). However, a clear discrepancy between the two data set are observed at the early stage of the recordings (March 13–17). During this period, the PM has a high amplitude (also the SM, Fig. 3c), while the observed H_s (in lagoon and offshore) remain low. We



Figure 3. (a) Significant wave height H_s recorded by the different oceanographic instruments along the West coast of La Réunion from 13 March to 5 May 2017. The offreef (blue line) and the midreef (magenta line) are derived from the pressure recorded off shore and in the lagoon, respectively. The Candhis (cyan) represents the wave gauge station located in Le Port (Fig. 1). The significant wave height (H_s) from the NOAA WWIII model is shown in red and extracted at node WW3 located on Fig. 1. Note that the vertical axes are not at the same scale, for the offreef and Candhis stations (on the left) and for the midreef pressure sensor (on the right). (b) Time-series of the wave height measured in the lagoon (magenta) and primary microseisms (PM) amplitudes (green dots) from seismic station SALI, filtered in the 10–20 s period band. (c) Time-series of the offreef wave height H_s (blue line) and secondary microseisms (SM) amplitudes (seismic data filtered in the 3–10 s period band), recorded at various seismic stations on La Réunion Island (colored points). The high amplitude of the SM between March 13 and 16 is related to the ending phase of the tropical storm Fernando.

interpret these observations as induced by the tropical storm Fernando, which was active from March 6 to 15 in the SW Indian Ocean and which passed close to Réunion Island on March 12 (http: //www.meteofrance.re/cyclone/saisons-passees). On March 13, the storm was already south of the island and continued escaping southward. We suggest that this storm was likely still generating SM noise close to 10 s period (observed throughout the whole Réunion island in both PM and SM bands), and a swell propagating towards the south which did not interact with the island. Therefore, the PM recorded by the station SALI from March 13 to 16 has likely a distant origin and was not generated locally by swell interacting with the coastal slope.

Fig. 3(c) shows that the measured SM amplitudes for different seismic stations on the island have the same pattern but with slightly different amplitudes from station to station. This indicates that the SM amplitude depends on the site effect near the station. A clear split in time between the elevated values of the SM and the local observed H_s (blue curves, Figs 3c and S4) is also observed. The delay times between the two parameters are proportional to the distance between the source location and the seismic station (discussed in Section 8). The recorded PM and SM amplitudes appear to depend not only on the strength of the storm that produced the swell and the distance between the source and the seismic station but also on a local site effect. For instance, the boxes A and B have similar SM amplitudes. However, the recorded H_s in box B (OFF H_s , Fig. 3c).

6 CORRELATING MICROSEISMIC AMPLITUDES WITH OBSERVED AND MODELLED WAVE HEIGHTS—TRANSFER FUNCTIONS

To determine the relationship between the local sea conditions and the microseismic noise, we correlate the RMS amplitude of the PM recorded at the seismic station SALI on land with the observed wave heights derived from the pressure sensors and the modelled wave heights from the WWIII model. Fig. 3(b) shows the PM amplitude variation together with the swell amplitude observed inside the reef (midreef H_s). This plot clearly displays good correlations between the two independent observables (except for the period when the tropical storm Fernando was still active), which we use below to determine transfer functions between microseismic noise amplitude and the wave height.

We focus here on the seismic station SALI which is the nearest to the oceanographic sensors (Fig. 1) and which has the largest RMS amplitude during the observing period. To discuss the correlation between the microseismic noise and the significant wave height, we take as an example in Fig. 4 the Austral swell occurring between 23 April and 2 May 2017 (box F, Fig. 3c). We chose this event, because of the presence of the LPSM and of the largest microseisms amplitudes. Figs 4(a) to (h) compare the observed and modelled wave height and the RMS amplitudes in the PM (upper row in Fig. 4) and in the LPSM (mid-row Fig. 4) noise bands for seismic station SALI. Microseismic noise is compared to observed H_s inside the reef (MID, midreef, Fig. 4 column I), outside the reef (OFF, offreef, Fig. 4 column II), northernmost off shore (at Candhis site, Fig. 4 column III) and to the modelled H_{sm} at node WW3 (Fig. 4 column IV). In these plots, each point represents an hourly measurement of the wave height and of the RMS microseismic noise amplitude.

As shown in Fig. 3(b), we observe a very good correlation between the wave heights and the PM amplitude during the observing period. The amplitude of the PM correlates with both the observed significant wave height derived from the OSSI wave gauges (MID, midreef and OFF, offreef) and the WWIII model, with Pearson correlation coefficient >0.95 (Figs 4a, b and d). These observations confirm that the PM relates to the local sea condition and is generated in the very coastal region, as suggested by previous studies (e.g. Barruol *et al.* 2006; Ardhuin *et al.* 2011). The correlation between the PM and the significant wave height at the northernmost CAND station is relatively lower, with Pearson coefficient correlation of 0.88 (Fig. 4c). As explained in the previous section (Section 5), this is due to the fact that the swell arriving from the SSW experienced refraction and energy reduction along its propagation path before being recorded at the Candhis wave buoy. This wave height reduction is clearly visible by comparing the swell height measured offreef (29 April 2017, Fig. 4b) and the maximum of swell amplitude of 2.4 m observed further north at Candhis (Fig. 4c).

The correlation between the amplitude of the LPSM and the significant wave heights for the different observations/model are plotted in Figs 4(e)–(h). These figures show how well the LPSM and the wave heights correlate with Pearson coefficient >0.9. These observations strongly favour that the observed LPSM is generated locally by the coastal reflected waves, which have been observed in other studies (e.g. Bromirski *et al.* 2005; Davy *et al.* 2016).

Figs 4(a)–(h) indicate that the microseism amplitudes at station SALI in both the PM and LPSM frequency bands correlate well and are linearly proportional to the significant wave heights measured in the ocean or derived from the numerical model WWIII. This suggests that these two parameters can be linked using a simple linear equation. Therefore, we used a linear regression technique to establish the transfer function between these parameters, that is between the different measured or modelled wave heights and the PM or LPSM amplitudes. In total, we determine 8 transfer functions shown in Figs 4(i)-(1). For each equation, the microseism amplitude and the wave height are in μ m and in m, respectively. Note that during our linear regression, we used a thresholds values of 0.15 and 1.0 μ m for the amplitude of the PM and LPSM, respectively. Therefore, the transfer functions are only valid for the microseism amplitudes above these values, which represent the recorded amplitudes when there is no swell activity.

The transfer functions between the PM noise amplitude (in green, Fig. 4) and the wave heights inside (MID, midreef) and outside (OFF, offreef) the reef, at the Candhis wave gauge and at the modelled WWIII point are $H_s = 0.95 * A_{PM} + 0.04$, $H_S = 6.78 * A_{PM} + 0.35$, $H_s = 2.77 * A_{PM} + 0.66$ and $H_s = 4.91 * A_{PM} + 0.86$, respectively. To validate these relations, we computed the wave height of the other swell events using the corresponding transfer function. Figs S5(a) to S5(d) show that the computed and the observed wave heights are comparable for the swell occurring between 21 and 25 March 2017 (box B, Fig. 3c) and Figs S5(e) to S5(h) for the swell occurring from 7 to 11 April 2017 (box C, Fig. 3c). This suggests that these equations are valid for any austral swell events and demonstrate that one can derive a reasonable estimate of the wave height from the terrestrial observation of the amplitude of the primary microseisms. This confirms that the PM amplitude is a good proxy of the coastal wave height and that a well calibrated seismic station can become a terrestrial wave gauge that can be useful in the absence of direct wave gauge in the ocean, which is the case of La Réunion Island. However, misfit between the observed and the computed wave heights are clearly observed for the 7-11 April swell event (box C, Fig. 3c), for station CAND (Fig. S5g). As discussed in Sections 4 and 5, the misfit between the two data sets may be due to the presence of additional swell recorded at the Candhis buoy only, which was strongly dissipated and did not generate PM. The presence of the swell from other source(s) is confirmed by the fact that only during these periods (April 7-11, box C, Fig. 3), Candhis station has the largest wave height amplitude.



Figure 4. RMS amplitude of the PM (top, a–d) and the LPSM (middle, e–h) together with the significant wave heights H_s from observations in the ocean (I, midreef, II, offreef and III, Candhis station) and from the WWIII swell models extracted at node WW3 (IV) for the period 22 April to 2 May 2017. For each plot, the left axis represents the amplitudes of the microseisms (in μ m) at station SALI and in the right axis the wave heights H_s (in m). *P* values indicate the Pearson coefficient for the correlations. Bottom (i–l): Transfer functions between the significant wave height H_s and the hourly RMS amplitude of the PM (green) and the LPSM (yellow). For each equation, A_{PM} and A_{LPSM} stand for primary and long-period secondary microseisms amplitude, respectively.

7 DIRECTIONS AND PERIODS OF SWELLS DEDUCED FROM SEISMIC NOISE

We present in Fig. 5(a) the hourly values of CpH and CpZ in the PM band, that is between 0.05 and 0.10 Hz, during the period 13 March and 5 May 2017 for station SALI, together with the H_s observed inside the reef (MID, midreef). This figure indicates that prior to the swell arrival, most of the CpH are dispersed between 0.6 and 1.0, while CpZ varies between 0.8 and 1.0. Both of these values clearly focus above 0.95 during the occurrence of the wave events (marked by the boxes). Strong polarization in both vertical and horizontal planes, indicates a strong linear polarization of the ground motion, similar to a horizontally propagating compressional P wave as described by Barruol *et al.* (2006) from near-shore seismic stations in French Polynesia islands.

The hourly measurements of the ground polarization azimuth at the coastal station SALI in the PM frequency band (0.05-0.10 Hz), together with the observed (ADCP D_p) and the modelled (WW3 D_{pm}) and D_{pms} for swell) azimuths are plotted in Fig. 5(b). The azimuths determined at the seismic station from polarization analysis (PM) are likely to be generated by the interaction of waves with the local bathymetry in the coastal area, and therefore, do not provide a measure of the direction of propagation of the swell at larger distance in the open ocean. In the following, we only referred to the azimuth values in the presence of swell activities (i.e. inside the boxes). Fig. 5(b) indicates a fairly good agreement between the swell peak directions issued from the model (D_{pms} , $\sim N015^{\circ}E\pm 5^{\circ}$) and the observed peak wave direction $(D_p, \sim N010^{\circ}E \pm 10^{\circ})$. It is accepted that low frequency swells can propagate to longer distance with minimal energy loss (e.g. Ardhuin et al. 2009), therefore, the similarity between these two parameters (observed peak wave



Figure 5. (a) Polarization parameters CpH (red dots) and CpZ (blue dots) measured on an hourly base in the PM, together with the wave height H_s measured in the lagoon (midreef, magenta line). Note that both polarization parameters (CpH and CpZ) are close to 1 for each swell event. (b) Plot of the polarization azimuths in the horizontal plane determined from the 3-D seismological data (green dots), and issued from oceanographic sensor ADCP (black dots) or from the WWIII model at the node WW3, swell peak wave direction (cyan dots) and wave peak direction for sea state (red dots).

direction nearshore and the modelled swells peak direction offshore) are not unexpected. The overall difference between the observed peak direction (D_p) and the modelled sea-state directions (D_{pm}) of around $\sim 25^{\circ} \text{E}\pm 15^{\circ}$ is due to the fact that the observed and the modelled peak wave directions do not relate to the same physical processes, since they are in coastal and deep water environments, respectively. The observations describe waves that have already been refracted, whereas the modelled waves have not been yet refracted and also include local wind-induced waves.

The azimuths measured from the seismic polarization analysis indicate a value equal to \sim N017°E±8°. The difference (\sim 10°) between the observed (D_p) and the computed azimuth (PM) is likely related to the swell progressive rotation when approaching the coast. As the swell interacts with relatively shallow bathymetry (half of the wavelength), the refraction process makes it progressively rotating and to finally propagate normal to the shoreline. Here, the estimated swell wavelength is around \sim 280 m (based on the modelled $T_{\rm pm}$ from the WWIII model), thus the waves likely start refracting at a depth of \sim 140 m and continue until a depth of \sim 14 m. This suggests that at the location of the ADCP (at \sim 20 m depth, OFF location Fig. 1), the swell has already begun to rotate and continues its rotation before breaking at the neighbouring reef crest.

A difference between the observed (\sim N005°E, Dp), the modelled (\sim N020°E, D_{pm}) and the computed azimuths (\sim N345°E) is observed for the swell in box F (i.e. April 28 to May 1). We propose that some of the reflected swells (from box E) propagated towards the south and may have interacted with the incoming waves, producing simultaneously PM and LPSM peaks. These waves hit the coastal area at the south of the SALI station, resulting in the obtained azimuth ~N345°E. The difference between the observed swell direction (N005°, D_p) and the modelled one (N025°E, D_{pm}) may suggest that the recorded directions by offreef (OFF) station (D_p) are partly related to the reflected swell from box E. Alternatively, the ADCP (D_p) and the WWIII modelled (WW3, D_{pm}) could have recorded different direction of the incident swells, as the waves propagate in many directions from the source.

The SM azimuths for the swells in boxes A, D and E (Figs 6 a and b), for SALI station, are estimated from seismic data polarization analyses to be N345°E, N045°E and N030°E, respectively (Fig. 6c). The azimuths for these swell events and for all seismic stations on La Réunion Island are presented on the map in Fig. 7. The computed azimuths in the secondary microseismic frequency band point towards to the storm where the swell is issued (Figs 6c and 7). The observed and modelled azimuths of wave propagation (ADCP D_p , WW3 D_{pm}) are however not comparable to the azimuths of the source location (SM polarization) because the local oceanographic observations are influenced by the local coastal geometry. Consequently it is not surprising that the modelled azimuths (D_{pm}) from the WWIII model (at the point WW3 at latitude 21°S and longitude 55°E, Fig. 1 and for other nodes in the south of the Island Fig. S6) indicate the presence of the swells that have direction of propagation \sim N010–030°E and do not appear to change much despite different source locations during the observing period. Hence, the



Figure 6. Examples of swell events, for station SALI. (a) Amplitude of the PM (green dots) and SM (yellow dots) and the midreef wave height (magenta line) measured in the lagoon for time interval in boxes A, D, E and F (Fig. 3c). Note that the amplitude of the PM is multiplied by a factor 5 to reach the same amplitude on the diagram as the SM. The *dt* shows the estimated delay time between the PM and SM. (b) Spectrograms of the vertical component of station SALI, together with the hourly swell frequency from the NOAA WWIII model (T_{pm} magenta dots) and recorded offshore (cyan dots). Black dots indicate ($2*T_{pm}$) to show the good fit with the increase of energy in the LPSM. PM and SM frequency bands are separated by the horizontal dashed line. (c) Maps of the *Hs* swell parameter issued from wave watch model WWIII on March 21 (left-hand panel), April 17 (middle panel) and April 23 (right-hand panel). Red circles show the distance between the seismic station in La Réunion Island and the SM sources. White stars indicate the approximate location of the SM source, determined from its distance and its measured incoming azimuth. Black arrows indicate the SM azimuth determined from the seismic polarization analysis.

SM azimuths cannot be related to local oceanographic observations nor modelled values. However, as we discuss in section 8, the SM azimuths (combined with its amplitude) can be used as precursory information for swell arrivals. The frequencies relative to the swell peak period (T_{pm}) from WWIII (Fig. 6, at the point WW3, latitude 21°S and longitude 55°E in Fig. 1) and the observed peak period (T_p) by the offshore station (OFF, Fig. 1) are superposed with the microseismic spectrum in



Figure 7. SM polarization azimuth measured at all seismic stations for the three swells presented in Fig. 6(c). It shows a very homogeneous pattern of polarization in this frequency band. Bathymetry isocontours are displayed by step of 200 m.

Fig. 6(b), for the swell events in boxes A, D, E and F. The observed (T_p) and modelled (T_{pm}) swells are similar and correlate well with the PM periods (Fig. 6b), suggesting that a coastal seismic station can be used to determine the swell's dominant period.

During any swell event, a clear peak in the PM frequency band between 0.05 and 0.10 Hz is observed (Fig. 2a), which corresponds to the swell frequency band. As presented in Section 4 and Figs 2(b) and (c), the presence of the long period secondary microseism (LPSM) is observed for the April 28 swell event. The spectrum in Fig. 6(b) for box F confirms the presence of such LPSM, which displays frequencies twice of the PM. We interpret such LPSM as generated by interaction between the incoming and the reflected swells, which creates standing waves near to the coastal areas. This likely induces a pressure recorded by the wave gauge and transformed into seismic waves, recorded by the seismic station, which confirms the near coastal source of the LPSM issued from swell coastal reflection, as suggested from previous works (e.g. Bromirski et al. 2005; Ardhuin et al. 2011). Bromirski et al. (2005) also suggested that the standing waves oscillate at twice the frequency of the incoming wave, such as the observed LPSM frequency here.

8 SM AS PRECURSORS OF STRONG SWELLS IMPACTING LA RÉUNION ISLAND

During the observing period (March 13 to May 5), SM often display a peak in amplitude preceding the actual arrival time of the H_s peak measured by the ocean sensor (Fig. 3c) and by seismic PM amplitude (Fig. 3b). In several cases, swells hit the coast (peak in the offreef H_s , Fig. 3c) $\sim 1-3$ d after the SM is recorded on-land at the seismic stations (boxes A, B, D and E, Figs 3c and 6a). Exception is observed during the period April 8–13 (box C, Fig. 3), while PM arrived a few hours before the SM, likely indicating the absence of causal relationship between them. Also, for box F, the (LP)SM and PM (Fig. 6a) were recorded at the same time favouring a (LP)SM source located close to the coast. Note also the presence of high SM amplitude (also PM amplitude but with low H_s) without any H_s followed, at the beginning of the recording (March 13–18). As discussed in Section 5, we interpret that these observations are related to the final stage of the tropical storm Fernando. On March 13, the cyclone was already at the south of the island and continued to propagate southward and was likely generating a swell propagating towards the south with a dominant period of 10 s. It is therefore likely that the PM recorded by the stations SALI had a distant origin and was not generated by a local swell, explaining thus the low H_s . Some examples of swell activities (boxes A, D, E and F in Fig. 3c) are presented in the following and are illustrated in Fig. 6.

Fig. 6(a) shows in greater detail that the maximum in SM amplitude (3–10 s, in yellow) measured at station SALI arrives before the PM peak (green dots) and the wave height peak (in the midreef station, in magenta). This can be explained by the signals associated with the SM travelling as a seismic wave in the solid Earth, whereas the PM is generated by ocean waves that travel across the ocean at much slower velocity. The SM is indeed generated within the active storm by the interaction of two swells of similar periods and can be recorded almost instantaneously at a seismic station, with delay time depending on the distance between the source and the seismic station. Assuming that the surface waves that dominate the SM propagate at \sim 3 km s⁻¹, they reach the station located thousands km away within few minutes. In the meantime, the swell generated by the same storm is accepted to travel at a velocity between 40 and 60 km hr⁻¹ depending on the wave period. At 50 km hr⁻¹ for instance, the swell may cross 1000 km of the ocean within 20 hr and for a distance of 4000 km (from La Réunion to a storm centre) will require more than 3 d of travel. This results in the observed delay times (dt in Fig. 6a) between the SM and the PM and/or Hs. The secondary microseisms can arrive simultaneously or shortly after the PM in case of near coastal sources of LPSM (box F, Fig. 6a)

or it may take few days (boxes A, B, D and E) for distant sources. Fig. 6(a) shows that for box A, the SM peak was estimated to be recorded 1 d and 18 hr before the PM peak, while for the box D, the time difference between the PM and the SM was estimated to be 3 d and 1 hr, suggesting a more distant storm. For box E, the PM peak arrived 2 d and 6 hr after the SM. The reflected swells from box E interfere with an incoming swell likely resulting in a near-coastal area source for the secondary microseisms (i.e. presence of LPSM). Thus, for box F (swell impacting La Réunion on 26 April 2017) the PM and SM (i.e. LPSM) arrived at the same time.

To estimate the SM source location, we first estimate its distance from the delay time between the PM and SM and the group velocity U(f), such as d = U(f) * dt (e.g. Chevrot *et al.* 2007), in which dt is the delay time (between PM and SM) and $U(f) = 3.6*g/(4*\pi*f)$, with g the gravitational acceleration (9.8 m² s⁻¹), and f is the wave frequency that can be determined from the slope of the PM (Fig. 6b). The constant 3.6 is used to convert the velocity into km hr⁻¹. Fig. 6(c) plots the possible SM source locations on the red circles, for each of the swells indicated in boxes A, D and E. Secondly, by performing a polarization analysis, we determine the incoming direction (azimuth) of the secondary microseisms. For station SALI, we obtained an azimuth of N345°E, N030°E and N040°E for boxes A, D and E, respectively (black arrows Fig. 6c). For each event, the intersection of the azimuth of incoming noise derived from the polarization analysis with the distance circle provides a rough approximation of the SM source location (white stars). We observe that in the three cases (boxes A, D and E), the white stars are in areas of maximum $H_{\rm s}$ parameters (yellow colours), indicating the SM source location is consistent with the swell activity (WWIII model) and that the maximum noise is generated in areas of maximum wave heights within the storms. We performed a polarization analysis for all stations in Fig. 1(a) and the computed azimuth for those stations, for the three swells (boxes A, D and E), are presented in Fig. 7. This Figure shows that all the stations consistently pointed to approximately towards the same sources: N345°E (box A), N030°E (box D) and N040°E (box E).

This simple analysis indicates first the feasibility of combining the delay time between the seismologically derived PM and SM peaks and the polarization analysis to locate the SM noise source. Secondly, this analysis also demonstrates that a continuous monitoring of the SM amplitude could be used to determine precursory information of the swell height that might impact the island few days later. Unfortunately, the SM data alone are not sufficient to predict the arrival time and the amplitude of the swell to hit the island. In order to carry out the prediction of the swell, the SM information could be combined with satellite data or wave forecasting models. Knowing the areas of the maximum H_s parameters in the oceans, one can estimate the arrival time of the PM and its strength and therefore, anticipate the impact of strong swell events on the island. The use of the SM could improve the accuracy of the existing models of swell forecasting (e.g. https://www.surf-forecast.com/) around the La Réunion Island. More generally, microseismic noise analysis will not only increase the number of ocean observations but will also be very useful in validating ocean wave models worldwide (e.g. Stopa et al. 2019).

9 CONCLUSIONS

This study shows that terrestrial seismic stations may represent alternative tools to improve swell observations, especially in regions of limited number of oceanographic sensors and in regions where cyclones and storms may render surface buoy deployments very hazardous. We demonstrate the reliability of using the microseismic noise recorded by land seismic stations as a swell proxy. We derive the significant wave height and period parameters (H_s and T_n) together with the wave direction (D_n) from pressure gauges and Acoustic Doppler Current Profiler (ADCP), respectively. These instruments were deployed on the ocean bottom in La Réunion nearcoastal areas and were operated in March-May 2017. The swell periods T_p were also retrieved from spectral analyses of the microseismic noise. Our results show that the swells measured on both sides of the reef display similar variations, but with an amplitude outside the reef about ten times higher than that inside, evidencing a strong reduction of the swell strength when crossing the reef crest, while preserving its frequency content. From the high correlation between the H_s and the primary microseisms (PM, 0.05-0.10 Hz) amplitudes (correlation coefficients >0.92), we established linear transfer functions between the two data sets that can be used for quantifying swell height from terrestrial seismic observations. A good correlation between the long-period secondary microseisms (LPSM, 0.10–0.15 Hz) and H_s is also observed in case of nearcoastal source of microseisms. The secondary microseisms (SM, 0.10-0.33 Hz) that develop within the storm at several thousands of km and that propagate as seismic waves in the solid Earth arrive ~ 1 -3 d before the swell hits the coast of La Réunion Island, indicating that SM may represent good precursors of an extreme swell event. We estimated the location of the SM source from the polarization analysis and the delay time between the arrival times of the PM and SM, which fits well with the WWIII wave height model. We therefore propose that continuous monitoring of SM may provide good precursory information for strong swells reaching the island, that can also be used to validate the existing forecasting global model around the island.

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SUPPORTING INFORMATION

Supplementary data are available at GJI online.

sm_Assessing_Swell_Reunion.pdf

Figure S1 Comparison between the Haiwaii/NOAA/NCEP and IFREMER wave models, (a) wave height H_s , (b) swell frequecy (period T_p) and (c) swell direction T_p .

Figure S2 Top panel: spectrograms of vertical component from 13 March to 5 May 2017 at station SALI. Rectangles show the swell that we analysed/discussed in this work (same as Fig. 2a). Bottom panel: time evolution of the PM (blue) and SM (red).

Figure S3 (a) Continuous line shows the significant wave height for the different oceanography stations (same as Fig. 3a). (b) Plot of the offreef versus midreef amplitudes showing the attenuation of the wave when crossed the reef.

Figure S4 PM (top panel) and SM (bottom panel) RMS amplitude for all seismic stations versus significant wave heights in the Lagoon (midreef) and offshore (offreef).

Figure S5 PM RMS amplitude (green dots) for SALI station versus wave heights for swells in boxes A and C (Fig. 3). The Observed wave heights for offreef (blue), midreef (magenta), Candhis (cyan) and from modelled WWIII (red) are plotted in continuous lines here. The dashed lines indicate the estimated wave heights using the transfer function from Section 6 and Fig. 4.

Figure S6 Plot of the polarization azimuths in the horizontal plane determined from the 3-D seismological data (green dots), and issued from oceanography sensor ADCP (black dots) or from the WWIII model at the different nodes S21°E55° (red dots), S21.5°E55° (cyan dots), S21.5°E55.5° (magenta dots) and S21.5°E56° (yellow dots). In general, the WWIII model at different nodes show a comparable direction.